Competing magnetic orderings and tunable topological states in two-dimensional hexagonal organometallic lattices

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The exploration of topological states is of significant fundamental and practical importance in contemporary condensed matter physics, for which the extension to two-dimensional (2D) organometallic systems is particularly attractive. Using first-principles calculations, we show that a 2D hexagonal triphenyl-lead lattice composed of only main group elements is susceptible to a magnetic instability, characterized by a considerably more stable antiferromagnetic (AFM) insulating state rather than the topologically nontrivial quantum spin Hall state proposed recently. Even though this AFM phase is topologically trivial, it possesses an intricate emergent degree of freedom, defined by the product of spin and valley indices, leading to Berry curvature-induced spin and valley currents under electron or hole doping. Furthermore, such a trivial band insulator can be tuned into a topologically nontrivial matter by the application of an out-of-plane electric field, which destroys the AFM order, favoring instead ferrimagnetic spin ordering and a quantum anomalous Hall state with a nonzero topological invariant. These findings further enrich our understanding of 2D hexagonal organometallic lattices for potential applications in spintronics and valleytronics.

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Since the discovery of the quantum Hall effect [1], the concept of topological order has become a subject of major interest in contemporary condensed matter physics [2]. Kane and Mele revealed [3] that graphene, a two-dimensional (2D) honeycomb lattice of carbon atoms [4], opens a gap by spin-orbit coupling (SOC) and realizes a topologically nontrivial state called the quantum spin Hall (QSH) state, giving rise to a quantized response of a transverse spin current to an applied in-plane electric field. This discovery triggers a huge amount of activities in exploring 2D or three-dimensional topological insulators (TIs) that possess robust helical conducting edge or surface states on the boundary of bulk insulators [5–10]. This peculiar helical state is topologically protected from elastic backscattering by time-reversal symmetry [9,10], and hence offers fascinating playgrounds for applications in spintronics and quantum computation devices [11].

Analogous to the quantum control of the spin [12,13], other binary quantum degrees of freedom such as two inequivalent valleys (K and K′ points) and two inequivalent lattice sites (A and B sublattices) in 2D hexagonal lattices, as shown in Fig. 1, have been exploited to bring the emergence of the so-called valleytronics [14–17] and pseudospintronics [17–19]. As the inversion symmetry is broken in 2D hexagonal structures, Bloch wave functions exhibit opposite Berry curvatures at K and K′ to host a quantum valley Hall (QVH) effect [16,20,21] characterized by a valley Chern number CV = CK − CK′.

Recently, various schemes have been proposed to generate valley currents in graphene [14,22,23] and 2D transition-metal dichalcogenides [24,25] by using their unique edge modes [14], defect lines [22], and strain [23]. Since a strong SOC gives rise to the interplay between spin and valley and lattice pseudospins [17], it is interesting and challenging to examine how it can rearrange the band structure and further change the topological property using external perturbations, e.g., electric field. Indeed, there have been several recent proposals on the topological phase transitions in 2D hexagonal structures, induced by an out-of-plane external electric field [26–28]. However, the realization of these exciting possibilities in 2D materials is still in its infancy.

So far, most of experimental and theoretical studies of topological physics have been concentrated on inorganic materials. The search for topological phases in organic materials is believed to open a new era in condensed matter physics, because of their advantages of low cost, easy fabrication, and mechanical flexibility. Here, we focus on a prototypical example of 2D hexagonal organometallic systems, triphenyl-lead (TL) lattice [29]. As shown in Fig. 1, Pb atoms form a honeycomb lattice with a threefold rotational symmetry by sharing phenyl bridges with three neighbors, and the A and B sublattices of Pb atoms exhibit slight buckling. Considering that the Pb atom has the 6s26p2 valence-electron configuration, one expects that the TL lattice would realize a QSH state, similar to silicene that is a buckled honeycomb lattice of Si [30]. Indeed, in their pioneering density-functional theory (DFT) studies of topological phases in organic systems [29,31], Wang, Liu, and Liu demonstrated that the TL lattice with a nonmagnetic configuration would be a QSH insulator.
In this Rapid Communication, we perform comprehensive DFT calculations for the TL lattice to investigate its true ground state by taking into account charge density wave (CDW) and spin density wave (SDW). We find that the antiferromagnetic (AFM) insulating state is more stable than the QSH and quantum anomalous Hall (QAH) states. Despite its topologically trivial feature, this AFM ground state possesses a novel electronic degree of freedom defined by the product of spin and valley indices, leading to Berry curvature-induced spin and valley currents under carrier doping or polarized optical pumping. We also reveal that the application of vertical gating induces a topological phase transition from the AFM insulating state by closing one of the valley gaps. As the gap reopens, the system enters into a ferrimagnetic QAH insulator with a Chern number of 1. Because the AFM and QAH states with fascinating electronic properties are connected by a single experimental knob and furthermore 2D organometallic systems are chemically flexible in terms of ligands and metal centers, the generic consequences of the present findings have much to offer for the design and development of spintronics and valleytronics applications.

We begin to study the nonmagnetic (NM) state of the TL lattice using the Perdew-Burke-Ernzerhof (PBE) calculation without the inclusion of SOC [32]. The optimized structure is displayed in Fig. 1. The calculated distance $d_{\text{Pb-Pb}}$ between two neighboring Pb atoms and their height difference $\Delta h$ are 7.432 and 2.932 Å, respectively. Here, each phenyl ring rotates along the Pb-Pb axis by $\sim 27^\circ$ relative to the horizontal plane of an isolated TL molecule. The PBE band structure shows Dirac cones at the $K$ and $K'$ points, with a Dirac point at the Fermi level $E_F$ [see Fig. 1S(a) of the Supplemental Material [33]]. On the other hand, when SOC is included in the PBE calculation, the band gap $E_g$ at $K$ and $K'$ is opened as high as $\sim 11$ meV [see Fig. 2(a)], in good agreement with that (8.6 meV) of a previous DFT calculation [29]. By computing the parity eigenvalues of Bloch wave functions at the time-reversal-invariant momenta, the NM state obtained using the PBE+SOC calculation is found to be a QSH state.

It is noticed that Pb atoms in the buckled TL lattice favor the $sp^3$ hybridization, leaving a single dangling bond on each Pb atom. Since the Dirac bands originating from such dangling-bond electrons have a small bandwidth of $\sim 0.5$ eV [see Fig. 2(a)], other electronic instabilities such as CDW or SDW may be favored over the QSH state [34]. For the CDW instability, we are unable to find its stabilization within the employed unit cell [see Fig. 1(a)], but the ferromagnetic (FM) and AFM states can be stabilized. The calculated PBE and PBE+SOC total energies of the FM and AFM states relative to the NM (or QSH) state are given in Table I. We find that, for the PBE (PBE+SOC) calculation, the FM state is less stable than the NM state by 6.8 (7.6) meV, while the AFM state is significantly more stable than the NM state by 37.4 (36.5) meV.

Figure 2(b) shows the PBE+SOC band structure for the FM state. We find that the SOC opens a gap of $E_g = 7.8$ meV at the two points near the $\Gamma$ point, while the PBE band structure shows a gap closing of the Dirac cones at $E_F$ [see Fig. 1S(b) of the Supplemental Material [33]]. From the PBE+SOC calculation, we find that the Fermi level lies well below the bottom of the Dirac cones, ensuring a large gap and a clear signature of a QSH state. The gaps near the Fermi level are calculated to be 2.86 and 3.03 meV, respectively. By comparing with the previous DFT result of 2.94 meV [28], our calculation shows a close agreement, with a small error likely due to the use of different DFT functionals.

In conclusion, we have investigated the electronic band structures of the TL molecule by performing DFT calculations with and without SOC. Our calculations show that the TL molecule exhibits a QSH state with a large gap of 37.4 meV, which is significantly more stable than the NM state. This QSH state is protected by both spin and valley symmetries and is expected to be robust against electronic instabilities such as CDW or SDW. The QSH state of the TL molecule may offer promising applications in spintronics and valleytronics due to its unique electronic properties and the chemical flexibility of organometallic systems.
TABLE I. Calculated total energies (in meV per Pb atom) of the FM and AFM states relative to the NM state, obtained using the PBE and PBE+SOC calculations. The calculated spin magnetic moments (in $\mu_B$) of Pb and C atoms are also given. Here, three C atoms bonding to Pb are taken.

<table>
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<th>PBE</th>
<th>PBE+SOC</th>
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<tr>
<td>FM</td>
<td>$\Delta E_{FM-NM}$</td>
<td>6.8</td>
</tr>
<tr>
<td></td>
<td>$M_{Pb}$</td>
<td>0.35</td>
</tr>
<tr>
<td></td>
<td>$M_{C}$</td>
<td>0.20</td>
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<tr>
<td>AFM</td>
<td>$\Delta E_{AFM-NM}$</td>
<td>-37.4</td>
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<tr>
<td></td>
<td>$M_{Pb}$</td>
<td>$\pm0.32$</td>
</tr>
<tr>
<td></td>
<td>$M_{C}$</td>
<td>$\pm0.16$</td>
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In the calculation, we calculate the Berry curvatures $\Omega$ whose integral over the Brillouin zone (see Fig. 2S of the Supplemental Material [33]) gives the Chern number $C = \frac{1}{\pi} \int_{BZ} \Omega d^2k = 1$, with equal contributions from the valley regions. The nonzero Chern number is the characteristic of a QAH state, similar to the recently studied triphenyl-manganese lattice [31].

It is remarkable that AFM order is stabilized in an organometallic compound composed of only main group elements. Contrasting with the QSH and QAH states in the TL lattice, the AFM state exhibits a large band-gap opening at valleys $K$ and $K'$ [see Fig. 2(c)]: i.e., the PBE calculation gives an identical value of $E_F = 469$ meV, while PBE+SOC gives different values of 481 and 457 meV, respectively. This large gap opening of the AFM state gives a large thermodynamic stability relative to the NM state (see Table I). To understand the underlying mechanism for the AFM spin ordering, we plot in Fig. 2(d) the PBE spin-polarized local density of states (DOS) projected onto the Pb atoms at the $A$ and $B$ sublattices, together with their spin characters. It is seen that the occupied (unoccupied) spin-up and spin-down dangling-bond states are localized at the $A(B)$ and $B(A)$ sites, respectively. Since electronic states with the same spin direction can hybridize with each other, the hybridization takes place between the occupied and unoccupied spin-up (spin-down) states localized at the $A(B)$ and $B(A)$ sites, respectively, yielding not only a gain of the exchange kinetic energy but also an insulating gap [35]. This kind of exchange interaction mediated by two electronic states which are energetically separated well below and above the Fermi level is characterized as a superexchange mechanism [36,37]. It is likely that such a superexchange interaction can be facilitated due to a considerable hybridization of the Pb $6p_z$ orbitals with the $\pi$ orbitals of neighboring phenyl rings. As shown in Fig. 3S of the Supplemental Material [33] and Table I, this hybridization is well represented by a large spin delocalization with the alternating spin densities of $\sim\pm0.32$ and $\sim\pm0.16 \mu_B$ for Pb atoms and C atoms in the phenyl ring, respectively.

In Fig. 2(c), the SOC-induced renormalization of the valley gaps in the AFM state can be described by the parameter $\delta$: that is, $E_{g,SOC} = \frac{2(m + \tau \delta)}{\epsilon_F}$, where $m = \frac{1}{2}E_F = 234.5$ meV is the mass term arising from the AFM spin ordering and $\tau = 1$ ($-1$) represents the valley index of $K$ ($K'$). The present value of $\delta = 6$ meV in the AFM state indicates a moderate spin-valley coupling (SVC), where the product $s \cdot \tau$ of spin and valley indices becomes a new degree of freedom of electrons. Here, the spin-up and spin-down bands remain degenerate because the Hamiltonian is invariant under simultaneous time reversal $T$ and spatial inversion $P$, although neither $T$ nor $P$ alone commutes with the Hamiltonian. Figure 3(a) (Fig. 4S of the Supplemental material [33]) shows the Berry curvatures of the lowest (highest) unoccupied (occupied) spin-up and spin-down bands, computed using PBE+SOC. It is seen that the spin-up and spin-down bands have the opposite values of $\Omega$ at valley $K$ and these values are also opposite to the corresponding values at $K'$, manifesting the SVC. Consequently, the Chern number becomes zero, and the insulating AFM state is characterized to be topologically trivial.

Due to the SVC in the AFM state, the valleys’ degeneracy can be lifted without any external field [21,38]. For instance, the valleys can be doped asymmetrically with electrons (or holes), as schematically illustrated in Fig. 3(a). In the case of electron doping, the conduction band is occupied to shift $E_F$ in are shown in (b), depending on the amount of doping level that shifts $\Delta E_f = m + 2\delta$ and $\Delta E_f > m + 2\delta$. Solid and dashed lines stand for the currents from $K'$ and $K$, respectively. The spin and valley indices $(s, \tau)$ are indicated in parentheses.

![Figure 3](image1)

![Figure 4](image2)
to a higher energy. If this shift $\Delta E_F$ is smaller than $m + 2\delta$, an applied in-plane electric field produces a transversal valley current with the electrons of $(s, \tau) = (\pm \frac{1}{2}, -1)$, giving rise to a net transversal spin current without charge current, as schematically shown in Fig. 3(b). This is characterized as the QVH effect. It is notable that such spin currents are induced by the spin-dependent Berry curvatures $\Omega_K$ [see Fig. 3(a)] that determine the anomalous velocities of Bloch electrons, $V_g \sim E^\infty \times \Omega_K$. For $\Delta E_F > m + 2\delta$, the pair of currents with $(s, \tau) = (\pm \frac{1}{2}, 1)$ start to contribute to a net transversal spin current in the reversal direction [see Fig. 3(b)]. When we switch from electron doping to hole doping, spin holes can generate valley and spin currents in the opposite directions. This generation of spin currents in the AFM state with time-reversal symmetry breaking represent the anomalous spin Hall effect.

The effective potential of the present AFM state can be characterized as a spin-dependent staggered lattice potential in the honeycomb lattice. It is evident that an additional spin-independent staggered lattice potential will induce a closure of the gap in one of the valleys, eventually giving rise to a nontrivial electronic topology. To explore this topological phase transition, we apply an out-of-plane electric field $E_{\text{out}}$ to produce a staggered electric potential in the buckled honeycomb TL lattice. Here, $E_{\text{out}}$ is simulated by superimposing an additional sawtooth potential along the $z$-direction with discontinuity at the midplane of the vacuum region of the supercell. This staggered electric potential is expected to lift the spin degeneracy of the AFM state because the occupied spin-up and spin-down dangling-bond states are localized at the $A$ and $B$ sites with different heights [see Fig. 2(d)], respectively. Consequently, as the magnitude of $E_{\text{out}}$ increases, the gap of the spin-split bands will decrease, close, and reopen at the $K$ and $K'$ points, leading to a topological phase transition. Indeed, our PBE+SOC calculations show the evolution of the band structure with increasing $E_{\text{out}}$, giving rise to a gap closing of the spin-down band at valley $K'$ for the critical field of $E_{\text{out}} = 0.62$ V/Å. Figure 4(a) shows the band structure and Berry curvature obtained at $E_{\text{out}} = 0.6$ V/Å. It is seen that the band gap at $K$ ($K'$) is much reduced as 119 (97) meV, compared to the value of 481 (457) meV in the absence of $E_{\text{out}}$ [see Fig. 2(c)]. The calculated spin magnetic moments for the Pb atoms at the $A$ and $B$ sites become $M_{\text{Pb(A)}} = 0.28\mu_B$ and $M_{\text{Pb(B)}} = -0.25\mu_B$, respectively, indicating a ferrimagnetic spin ordering. We note that the Chern number for this ferrimagnetic state is still zero. By contrast, for $E_{\text{out}} = 0.7$ V/Å [39], the Chern number is changed into 1 as a consequence of the band inversion at valley $K'$ where the sign of Berry curvature changes [see Fig. 4(b)]. Here, the spin magnetic moments for the Pb atoms are much reduced as $M_{\text{Pb(A)}} = 0.18\mu_B$ and $M_{\text{Pb(B)}} = -0.15\mu_B$. These results obviously indicate a phase transition to a topologically nontrivial QAH state with ferrimagnetic order. It is noticeable that, when $E_{\text{out}}$ is above $\sim 0.71$ V/Å, the gap of the spin-down band at valley $K$ closes and reopens, which makes the system back to a trivial insulator. Since 48 i.e., the gap difference between $K$ and $K'$ valleys in Fig. 2(c) amounts to 24 meV, the topological nontrivial QAH state induced by a certain out-of-plane external electric field may be realized at temperatures below $\sim 300$ K.

In summary, we have performed comprehensive DFT calculations for the hexagonal TL lattice to investigate its true ground state by considering the QSH and QAH states as well as a band insulator with AFM order. We find that the topologically trivial AFM band insulator is more stable than the QSH and QAH states. This AFM state gives an emergent electronic degree of freedom characterized by the product of spin and valley indices, which leads to Berry curvature-induced spin and valley currents under electron or hole doping. Furthermore, we find that the application of an out-of-plane electric field can induce a quantum phase transition from the AFM state to a topologically nontrivial QAH state with ferrimagnetic order. Our findings are fairly generic for 2D organometallic lattices, which will provide novel platforms for the applications of spintronics and valleytronics using 2D AFM hexagonal lattices. In particular, the two building blocks of metal center and ligand in 2D organometallic lattices are two variables in their syntheses, which can influence the strength of spin-orbit coupling, electron hopping parameter, and onsite Coulomb repulsion. This aspect of 2D organometallic lattices will surely enrich the exploration of topological and correlated electronic phases. The theoretical exploration of such a fascinating regime will be a subject of future work.

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[31] The present DFT calculations were performed using VASP [G. Kresse and J. Hafner, Phys. Rev. B 48, 13115 (1993); G. Kresse and J. Furthmüller, Comput. Mater. Sci. 6, 15 (1996)] with the projector-augmented wave method and a plane-wave basis set. For the treatment of exchange-correlation energy, we employed the generalized-gradient-approximation functional of PBE [J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996)]; the TL lattice was modeled by a periodic slab geometry with ~25 Å of vacuum in between the slabs. Here, we used the optimized lattice constant a₀ = 11.866 Å obtained using the PBE calculation with SOC. A plane-wave basis was employed with a kinetic energy cutoff of 400 eV, and the k-space integration was done with the 9 x 9 Monkhorst-Pack meshes in the Brillouin zone. We employed a dipole correction that cancels the artificial electric field across the slab [J. Neugebauer and M. Scheffler, Phys. Rev. B 46, 16067 (1992)].


[33] As another candidate of the ground state, one may consider a Mott-Hubbard insulator driven by strong on-site Coulomb repulsion. However, since the AFM ordering between neighboring Pb dangling-bond spins is attributed to superexchange interactions mediated by a considerable hybridization of the Pb 6p orbitals with the π orbitals of neighboring phenyl rings (as discussed below), such a possibility of the Mott-Hubbard insulator is unlikely in the present system.


[38] According to previous experiments [Y. Zhang, T. Tang, C. Girit, Z. Hao, M. C. Martin, A. Zettl, M. F. Crommie, Y. R. Shen, and F. Wang, Nature (London) 459, 820 (2009); K. F. Mak, C. H. Lui, J. Shan, and T. F. Heinz, Phys. Rev. Lett. 102, 256405 (2009)] it was observed that the application of an electric field of ~0.7 V/Å closes the band gap of ~100–250 meV. Considering the fact that the change of the band gap in bilayer graphene was observed to be almost proportional to external electric field, the present prediction that an out-of-plane electric field of ~0.7 V/Å closes the band gap of ~480 meV is well comparable to the experimental result of bilayer graphene.